


Chapter 10

Capacitors and Capacitance

 Source: Circuit Analysis: Theory and Practice ©Delmar Cengage Learning

Capacitance of a Parallel-Plate Capacitor

$$C = \epsilon A / d$$

- Directly **proportional to** plate area ***A***
- **Inversely proportional to** plate separation ***d***
- **Dependent on dielectric ϵ**
- $\epsilon = \epsilon_r \epsilon_0$, $\epsilon_0 = 8.854 \times 10^{-12} \text{F/m}$
- A farad(**F**) is a very large unit, e.g., μF or pF

Example

Compute the capacitance of a parallel-plate capacitor with plates 10cm by 20cm, separation of 5mm, and a mica dielectric. ($\epsilon_0=8.854 \times 10^{-12} \text{F/m}$)



Capacitor Voltage Rating

Capacitors rated for **maximum operating voltage** (**Working Voltage dc** or **WV**)

- Rating is necessary due to dielectric breakdown



G = $\pm 2\%$
J = $\pm 5\%$
K = $\pm 10\%$
M = $\pm 20\%$



Capacitor2_10pF



Capacitor1_100uF



4

Capacitors in Parallel

- **Total charge** on capacitors is **sum of all charges**
 $Q = CV, Q = C_T E = C_1 V_1 + C_2 V_2 + C_3 V_3$
- **All voltages are equal, $E = V_1 = V_2 = V_3$**
- **Total capacitance C_T of capacitors in parallel**
 - **Sum of their capacitances** (like resistors in series)
 $C_T = C_1 + C_2 + C_3$



Capacitors in Series

- **Same charge** appears on all capacitors $Q = Q_1 = Q_2 = Q_3$
- Total V : Sum of individual voltages $E = V = V_1 + V_2 + V_3$
- $C_T = 1 / (1/C_1 + 1/C_2 + 1/C_3)$ (like resistors in parallel)



Voltage Divider for Capacitors in Series

$$E = V_1 + V_2 + V_3$$

$$Q = Q_1 = Q_2 = Q_3$$
$$= C_1 V_1 = C_2 V_2 = C_3 V_3$$

Smaller C to get Larger V

Energy Stored by a Capacitor

- A capacitor does **not dissipate power**
- **Stored energy**: When power is transferred to a capacitor, $W = C V^2 / 2$

Capacitor Failures and Troubleshooting

- Reasons for capacitor's failure
 - **Excessive voltage, current, or temperature, or aging**
- Test with an ohmmeter
 - **Good capacitor will read low, then gradually increase to infinity**
- Capacitor short
 - Meter resistance will stay low
- If capacitor is leaky
 - Reading will be lower than normal
- If capacitor is open
 - Stays at infinity

Kernel abilities

1. Can give the definition of capacitance for a capacitor.
2. Can distinct all the different types of capacitors.
3. Can calculate the total capacitance of capacitors in series-parallel circuits.
4. Can understand the voltage divider for capacitors in series-parallel circuits.
5. Can understand the capacitor voltage and current during charging.